

تفريغ تحليل آبي

IR اسم الموضوع:

إعداد الصيدلاني / ة: نور منصور



Harmonic Oscillator Vibrational Frequency

The natural frequency of the oscillation is

$$\nu_m = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

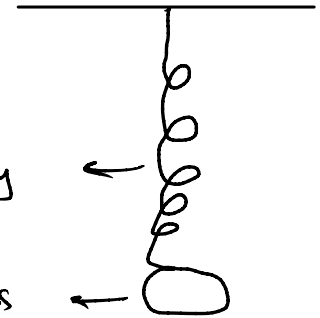
ν_m = natural frequency

m = mass of the attached body

k = force constant of the spring

(bond) spring

(atom) mass



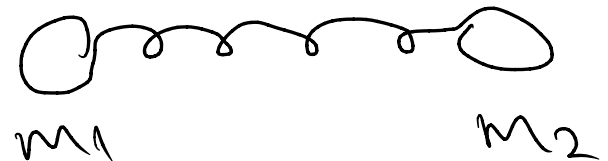
- The equation may be modified to describe the behavior of a system consisting of two masses m_1 and m_2 connected by a spring.

- it is only necessary to substitute the reduced mass μ for the single mass m , where

← من الذريتين المرتبطتان مع هذا spring او bond

* اقل molecule مكون من 2 atoms.

بعضها بدل m في القانون ← $\mu = \frac{m_1 m_2}{m_1 + m_2}$



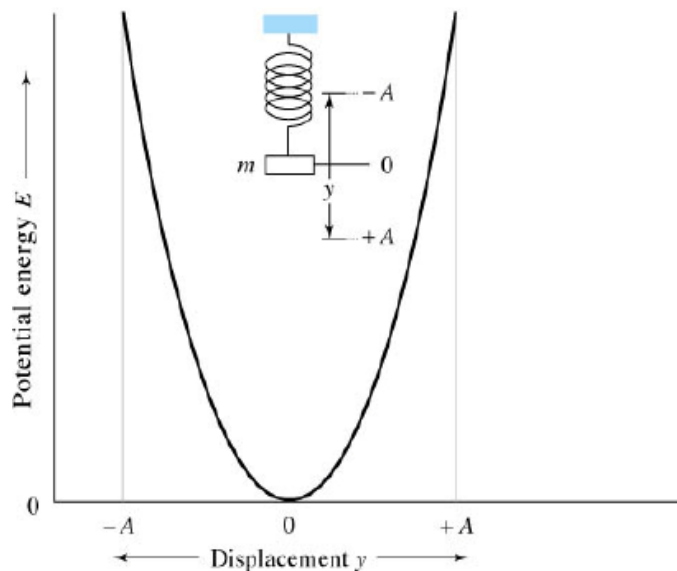
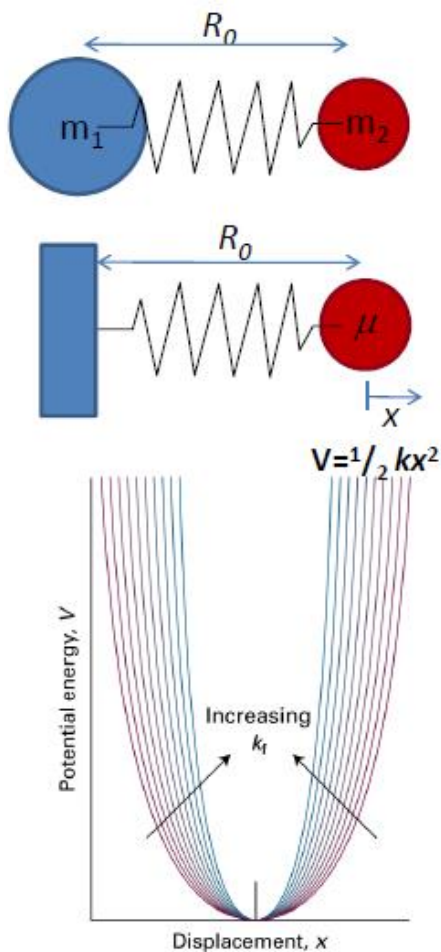
The equation may be modified to describe the behavior of a system consisting of two masses m_1 and m_2 connected by a spring. Here, it is only necessary to substitute the reduced mass μ for the single mass m where

$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$

Thus, the vibrational frequency for such a system is given by

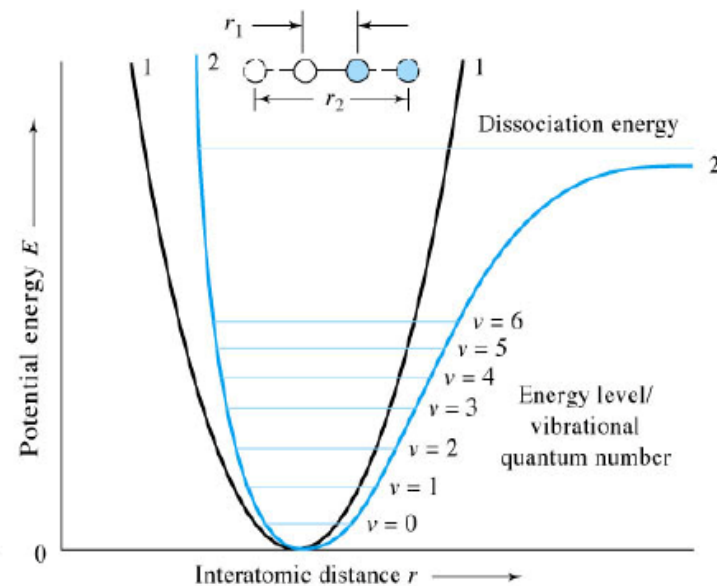
$$\nu_m = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} = \frac{1}{2\pi} \sqrt{\frac{k(m_1 + m_2)}{m_1 m_2}}$$

$\xrightarrow{\mu} \frac{m_1 m_2}{m_1 + m_2}$



(a)

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(b)

FIGURE 16-3 Potential-energy diagrams. (a) harmonic oscillator. (b) Curve 1, harmonic oscillator; curve 2, anharmonic motion.

- Quantum Treatment of Vibrations

$$\Delta E = h \nu_m = \frac{h}{2\pi} \sqrt{\frac{k}{\mu}}$$

$$E_{\text{radiation}} = h \nu = \Delta E = h \nu_m = \frac{h}{2\pi} \sqrt{\frac{k}{\mu}}$$

The radiation in wavenumbers,

$$\bar{\nu} = \frac{1}{\lambda}, \quad \lambda = \frac{c}{\nu} \rightarrow \bar{\nu} = \frac{\nu}{c} \rightarrow \nu = c \cdot \bar{\nu} \rightarrow \bar{\nu} = \frac{\nu}{c}$$

$$\bar{\nu} = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} = 5.3 \times 10^{-12} \sqrt{\frac{k}{\mu}}$$

Where, ν is the wavenumber of an absorption peak in cm^{-1} , k is the force constant for the bond in newtons per meter (N/m), c is the velocity of light in cm/s, and the reduced mass μ has units of kg. k has been found to lie in the range between 3×10^2 and 8×10^2 N/m for most single bonds, with 5×10^2 serving as a reasonable average value. Double and triple bonds are found by this same means to have force constants of about two and three times this value (1×10^3 and 1.5×10^3 , respectively).

The radiation in wavenumbers

$$C = \lambda \times \nu \Rightarrow \bar{\nu} = \frac{1}{\lambda} = \frac{\nu}{C}$$

$$\bar{\nu} = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} = 5.3 \times 10^{-12} \sqrt{\frac{k}{\mu}}$$

$$\Delta E = h\nu_m = \frac{h}{2\pi} \sqrt{\frac{k}{\mu}}$$

$$\Rightarrow \nu_m = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}$$

ν : wavenumber of an absorption peak in cm^{-1}

k : the force constant for the bond in newtons per meter (N/m)

C : the velocity of light in cm/s

μ : the reduced mass has in kg.

k : in the range between 3×10^2 and 8×10^2 N/m for most single bonds, with 5×10^2 serving as a reasonable average value.

Double and triple bonds are found by this same means to have force constants of about two and three times this value (1×10^3 and 1.5×10^3 , respectively).

Example:

Calculate the approximate wavenumber and wavelength of the fundamental absorption peak due to the stretching vibration of a carbonyl group C=O.

Solution:

1 mole $\rightarrow 6 \times 10^{23}$ atoms
MW C = 12 g
MW O = 16 g

double
 $k = 1 \times 10^3$

Mass of C is $m_1 = 12 \times 10^{-3} \text{ kg/mol} / 6 \times 10^{23} \text{ atom/mol}$
 $= 2 \times 10^{-26} \text{ kg}$

Mass of O is $m_2 = 16 \times 10^{-3} / 6 \times 10^{23} = 2.7 \times 10^{-26} \text{ kg}$

And the reduced mass μ is given by:

$$\mu = \frac{m_1 m_2}{m_1 + m_2} = (2 \times 10^{-26}) \times (2.7 \times 10^{-26}) / (2 + 2.7) \times 10^{-26}$$
$$= 1.1 \times 10^{-26} \text{ kg}$$

As noted earlier, the force constant for the typical double bond is about $1 \times 10^3 \text{ N/m}$. substituting this value and μ into

$$\text{wavenumber} = \bar{\nu}_m = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} = 5.3 \times 10^{-12} \sqrt{\frac{k}{\mu}}$$

$\nearrow 1 \times 10^3$
 $\searrow 1.1 \times 10^{-26}$

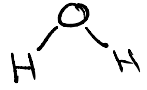
$$= 1.6 \times 10^3 \text{ cm}^{-1} = 1600 \text{ cm}^{-1}$$

And the stretching band is found experimentally to be in the region of 1600 to 1800 cm^{-1}

* قم عدد VM في 0 = 9
 $3N - 5 \rightarrow 8 + 2 - 5 = 1$

Vibrational Modes

– Number of possible modes



• Nonlinear molecule: $3N - 6$



• Linear molecule: $3N - 5$

← هنا كل atom بقدر هل 3 درجات حركه
 1- vibration 2- rotation 3- translation

* كل molecule ال vibrational mode

يختلف عن التالي حسب :-

① عدد atom ال موجود على molecule

② هل molecule linear ← لا

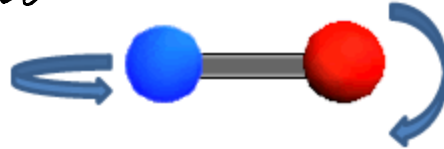
3 درجات حركه 3 degrees of freedom – i.e., 3 coordinates in space

3 translations and 3 rotations account for 6 motions of molecule

– Rotation about center bond in linear molecule is indistinguishable

ما يقدر الارقام

← يعني 3 translation 2 rotation



– Remaining degrees of motion represent vibrational motion (i.e., number of vibrations within the molecule)

Calculate Number of Vibrational Modes

The degrees of vibrational modes for **linear** molecules can be calculated using the formula:

$$3n - 5 \text{-----}(1)$$

The degrees of freedom for **nonlinear** molecules can be calculated using the formula:

$$3n - 6 \text{-----}(2)$$

n is equal to the number of atoms within the molecule of interest.

The following procedure should be followed when trying to calculate the number of vibrational modes:

1- Determine if the molecule is linear or nonlinear (i.e. Draw out molecule using VSEPR). If linear, use Equation 1. If nonlinear, use Equation 2

نظرية تستخدم للكثير الشكل الهندسي
للصريح في الفراغ (linear or not)

2- Calculate how many atoms are in your molecule. This is your n value. Plug in your n value and solve.

Example 1: CS₂

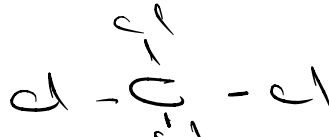


An example of a **linear** molecule would be CS₂. There are a total of 3 atoms in this molecule. Therefore, to calculate the number of vibrational modes, it would be:

$$3(3)-5 = 4 \text{ vibrational modes.}$$

dipole moment μ

Example 2: CCl₄



CCl₄ is a **nonlinear** molecule. In this molecule, there are a total of 5 atoms.

Therefore, there are $3(5)-6 = 9$ vibrational modes.

ولكن هذا المثال في الواقع يظهر استثناء عن القاعدة

Example 2: H₂O



H₂O is a **nonlinear** molecule. In this molecule, there are a total of 3 atoms.

Therefore, there are $3(3)-6 = 3$ vibrational modes.

How many vibrational modes?

2 atoms (H_2) - 1 vibration (~~stretch ν~~)



3 atoms (H_2O) - 3 vibrations (~~ν_s, ν_{as}, σ~~)



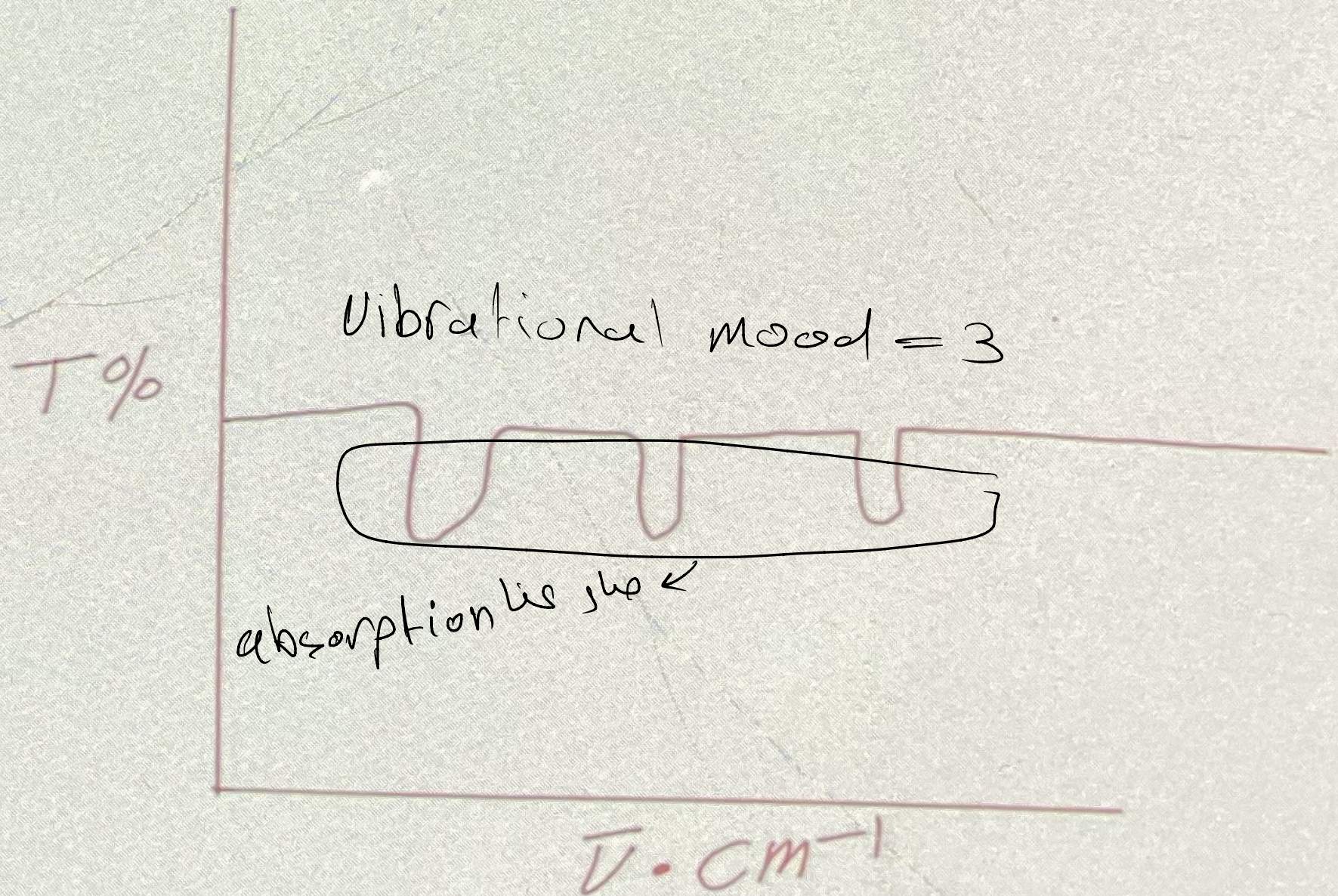
3 atoms (CO_2) - 4 vibrations (~~$\nu_s, \nu_{as}, \sigma, \omega$~~)



4 atoms (H_2CO) - 6 vibrations (~~$\nu_s, \nu_{as}, \sigma, \omega, \rho(\text{CH}_2), \nu(\text{C}=\text{O})$~~)



peaks, spectrum IR ν VibrationaL MoOd



Factors Influence the Normal Modes

عدد الذرات إلى مجمل molecule

Four factors tend to produce **fewer experimental peaks** عدد أقل من المتوقع

than would be expected from the **theoretical** number of

normal modes. ^{٤٥٢ ٤٥٢} (1) the symmetry of the molecules is such

that no change in dipole results from a particular vibration;

→ Wave number التردد 

(2) the energies of two or more vibrations are identical or

nearly identical; (3) the absorption intensity is so low as to

be undetectable by ordinary means; ^(٤) or the vibrational

energy is in a wavelength region **beyond** the range of the

instrument

عدد الذرات إلى مجمل molecule
 peak تظهر خارج Range الجهاز

Fewer and more experimental peaks than calculated

- Fewer peaks

- (1) the symmetry of the molecules is such that no change in dipole results from a particular vibration
- (2) the energies of two or more vibrations are identical or nearly identical
- (3) the absorption intensity is so low as to be undetectable by ordinary means

- More peaks → بنلاحظ peaks أكثر من المتوقع

(1) Overtone

(2) Combination bands

Fundamental Peaks and Overtones

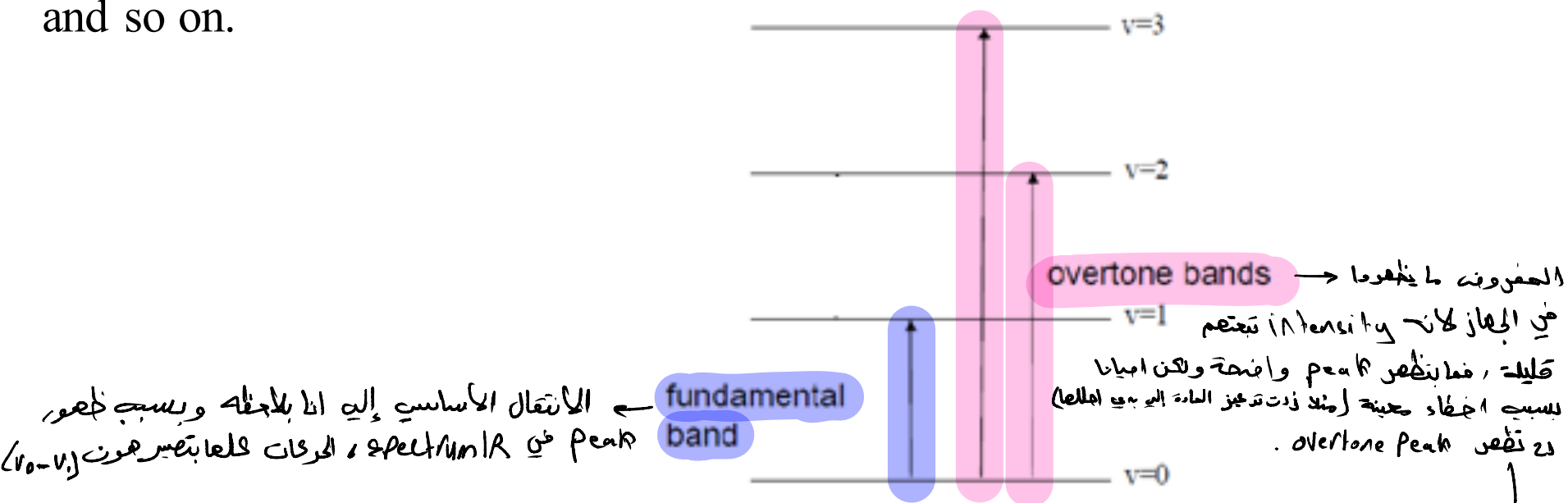
Fundamental transition:

The excitation from the ground state V_0 to the first excited state V_1 is called the fundamental transition. It is the most likely transition to occur.

Fundamental absorption bands are strong compared with other bands that may appear in the spectrum due to overtone, combination, and difference bands.

Overtone bands:

Result from excitation from the ground state to higher energy states V_2 , V_3 , and so on.



- If the fundamental absorption occurs at frequency ν , the overtones will appear at about 2ν , 3ν , and so on.
- Overtones are weak bands and may not be observed under real experimental conditions.

* Fundamental band و Overtones

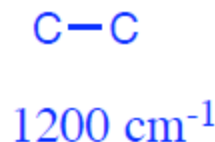
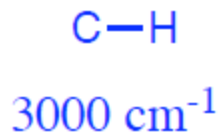
Coupling modes: إذا overtone ظهرت في Peak مع coupling
 فـ ν_3 فينتجوا مع بعض وينتجوا Frequency، و ν_1 و ν_2 تظهر على شكل Peak زيادة عن ν_1 و ν_2 حاسبينها.

- Vibrating atoms may interact with each other. **Two vibrational frequencies** may couple to produce a new frequency $\nu_3 = \nu_1 + \nu_2$. The band at ν_3 is called **a combination band**.
 new peak ← ν_3 ← ν_1 (Fundamental band) + ν_2 (overtone) ← ν_3
- If two frequencies couple such that $\nu_3 = \nu_1 - \nu_2$, the band is called **a difference band**.
- Not all possible combinations and differences occur.

Factors that affect the frequency of light absorbed

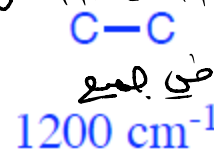
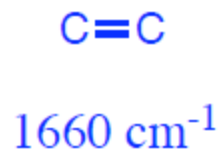
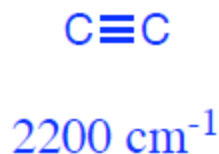
or Wavenumber

1. Bonds which have one lighter and one heavier atom vibrate faster than bonds which have two heavier atoms.

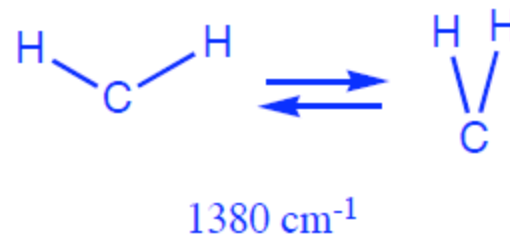
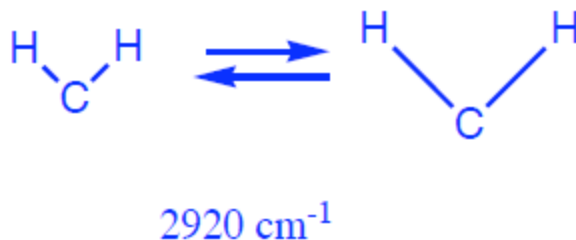


2. Stronger bonds vibrate faster than weaker bonds.

* قلنا قبل انه single bond البها
اعلى Wavenumber ولكن كانت الرتبة
فيها H مثل C-H, X-H, O-H
ولكن عندما تقارن C-C في جميع
انواع الروابط لانه اقل
Wavenumber لها single bond

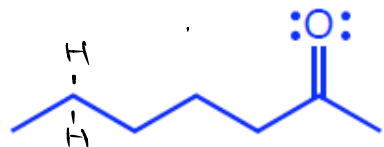


3. Stretching vibrations are faster than bending vibrations

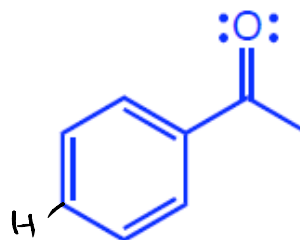


Factors that affect the amount of light that is absorbed

1. If there are many C-H bonds in a molecule absorbing light at the same frequency, the band will be much larger than if there are only a few.

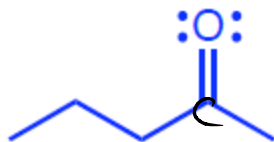


lots of C-H bonds
large absorption



fewer C-H bonds
smaller absorption

2. Strength of the dipole - bonds which have a strong dipole moment will absorb light more strongly than those which have a weaker dipole moment.



C=O very polar, strong dipole
large absorption



C=C nonpolar, small dipole
small absorption



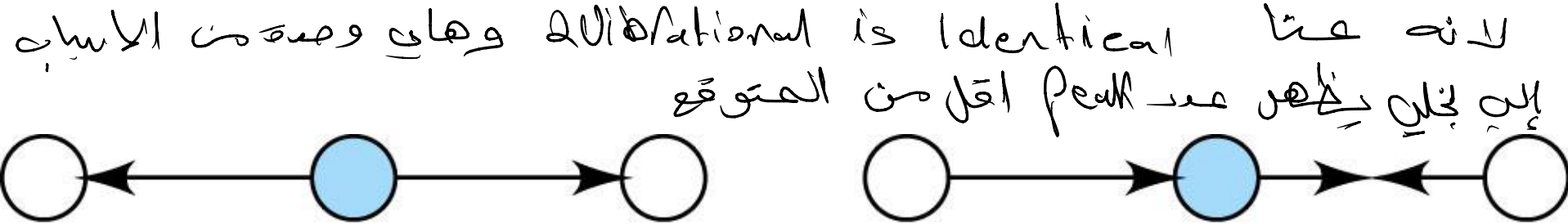
CO₂ Molecule

Let us consider the infrared spectrum of carbon dioxide. If no coupling occurred between the two C=O bonds, an absorption peak would be expected at the same wavenumber as the peak for the C=O stretching vibration in an aliphatic ketone (about 1700 cm⁻¹). Experimentally, carbon dioxide exhibits two absorption peaks, the one at 2330 cm⁻¹ and the other at 667 cm⁻¹. Carbon dioxide is a linear molecule and thus has $3 \times 3 - 5 = 4$ normal modes. Two stretching vibrations are possible. The symmetric vibration causes no change in dipole. Thus, the symmetric vibration is infrared inactive.

The asymmetric vibration produce a change in dipole moments, so absorption at **2330** cm^{-1} results.

The remaining two vibrational modes of carbon dioxide involve ^{bending} **scissoring**. The two bending vibrations are the resolved components at 90 deg to one another of the bending motion in all possible planes around the bond axis. The two vibrations are identical in energy and thus produce a single peak at **667** cm^{-1} .

symmetric و 4 بطن CO_2 4 vibrational modes
(2330, 667) 2 Peaks يفرع عن 2 بطن و 2 بطن stretching



Symmetric

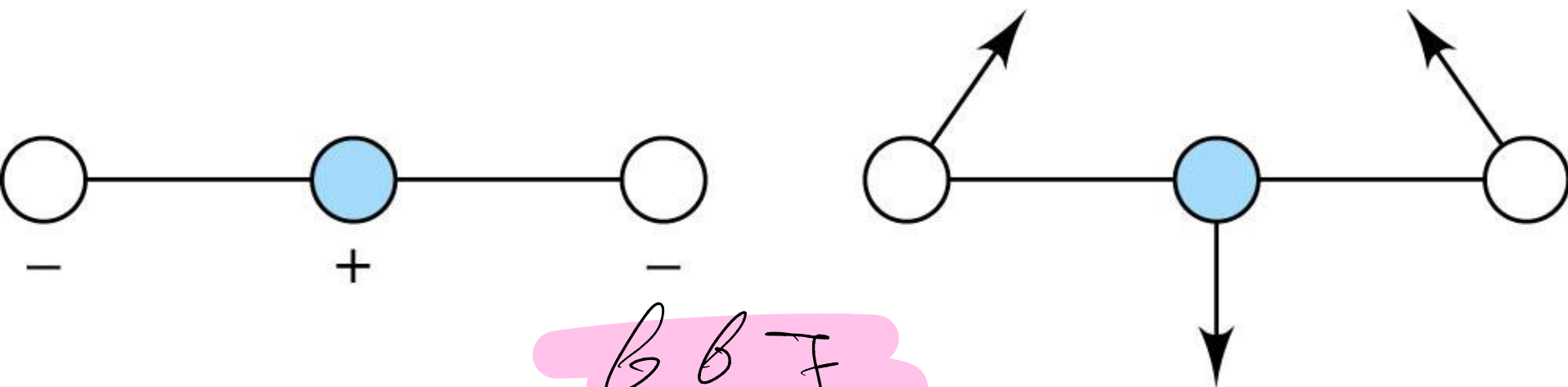
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inactive

Stretching

Asymmetric

2330



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667

Bending

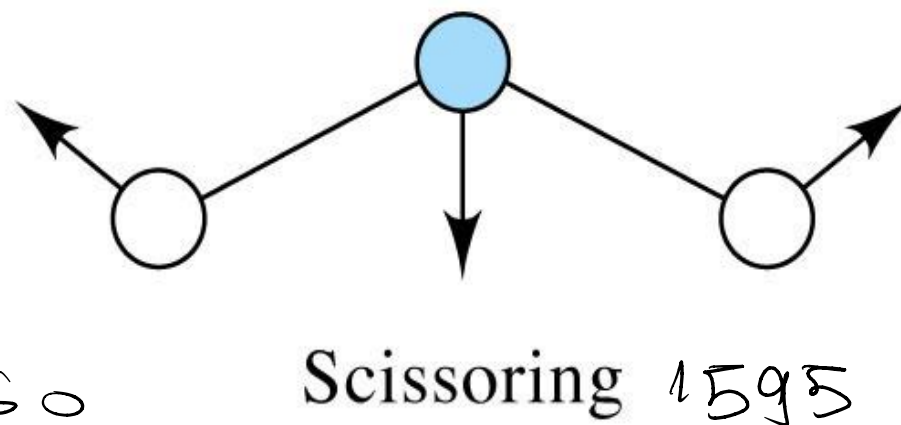
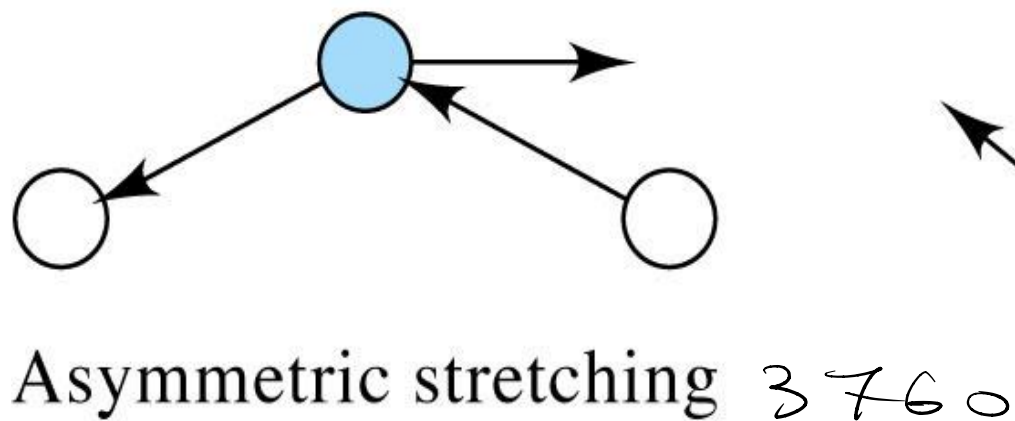
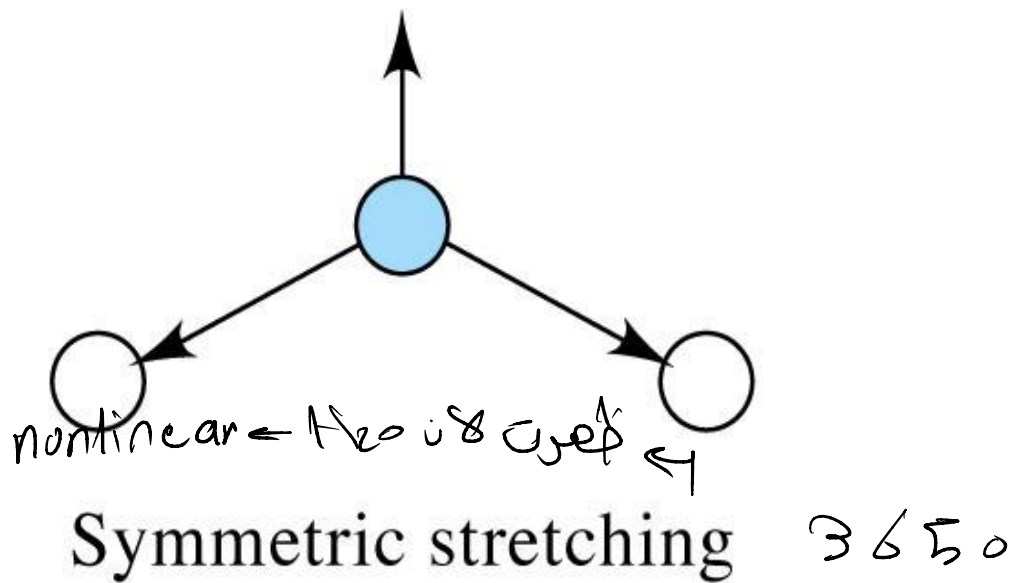
H₂O molecule

Triatomic molecule such as water, sulfur dioxide, or nitrogen dioxide have $3 \times 3 - 6 = 3$ vibrational modes. The central atom is not in line with the other two, a symmetric stretching vibration will produce a change in dipole and will thus be responsible for infrared absorption.

Stretching peaks at ^{symmetric}3650 and ^{asymmetric}3760 cm⁻¹ appear in the infrared spectrum for the symmetric and asymmetric vibrations of the water molecule.

There is only one component to the scissoring vibration for this nonlinear molecule. For water, the bending vibration cause absorption at 1595 cm⁻¹.

scissoring (bending) ↓



INFRARED SOURCES

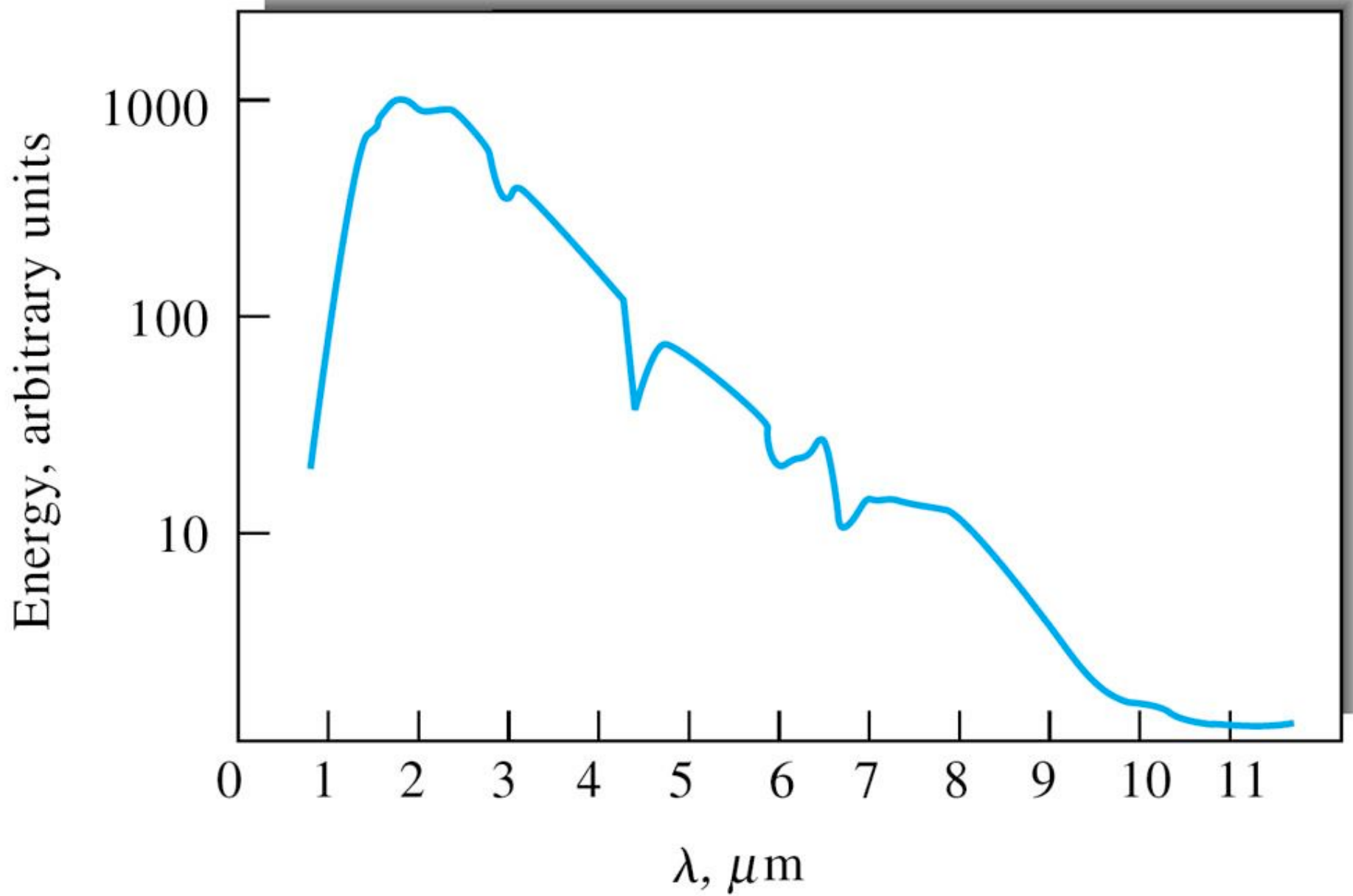
- **Sources**

لأشعة تحت الحمراء

Infrared sources consist of an inert solid that is heated electrically to a temperature between 1500 and 2200 K. Continuum radiation approximating that of a blackbody results. The maximum radiant intensity at these temperatures occurs between 5000 to 5900 cm^{-1} .

- **The Nernst Glower:** The Nernst glower is composed of ^{أكاسيد الأرض النادرة} rare earth oxides ^{أسطوانة} formed into a cylinder having a diameter of 1 to 2 mm and a length of perhaps 20 mm. Platinum leads are sealed to the ends of the cylinder to permit electrical connection to what amounts to a resistive heating element. As current is passed through the device, temperature between 1200 K and 2200 K

result. * صفيحة أو الأسطوانة من البلاتين أو الرصاص، يتسخن عن طريق الكهرباء والتسخين ينتج حرارة بمقدار 1200-2200 K إلى بضع آلاف درجة مئوية (5000-5500 °C)



- The Global Source:** A Global is a silicon carbide rod, usually about 50 mm in length and 5 mm in diameter. It also is electrically heated (1300 to 1500 K). Spectral energies of the Global and the Nernst glower are comparable except in the region below $5\mu\text{m}$, where the Global provides a significantly greater output.
 ← بظرف output اسیس کنٹارکٹ
- Incandescent Wire Source:** A source of somewhat lower intensity but longer life than the Global or Nernst glower is a tightly wound spiral of nichrome wire heated to about 1100 K by an electrical current.
 نیکل + کروم
 ← سلاخ طاقوف لیکل ملزوی

- **The Mercury Arc:** For the far-infrared region of the spectrum ($\lambda > 50 \mu\text{m}$), none of the ^{من قبل} thermal sources just described provides sufficient radiant power for convenient detection. Here, ^{قوس زئبقی} a high-pressure mercury arc is used. This device consists of a ^{جهاز ضغط بالكم ارتد} quartz-jacketed ^{في انموسفير} tube containing ^{من ضغط بالكم ارتد} mercury vapor at a pressure greater than one atmosphere. Passage of electricity through the vapor forms an internal plasma source that provides continuum radiation in the far-infrared region.

- **The Tungsten Filament Lamp:** An ordinary tungsten filament lamp is a convenient source for the near-infrared region of 4000 to 12,800 cm^{-1} .

← قابل للتعديل

- **The Carbon Dioxide Laser Source:** A tunable carbon dioxide laser is used as an infrared source for monitoring the concentrations of certain atmospheric pollutants and for determining absorbing species in aqueous solutions. A carbon dioxide laser produces a band of radiation in the 900 to 1100 cm^{-1} range.

Handwritten signature

Sources

Nernst Glower	heated rare earth oxide rod (~1500 K)	1-10 μm
Globar	heated SiC rod (~1500 K)	1-10 μm
W filament lamp	1100 K	0.78-2.5 μm
Hg arc lamp	plasma	>50 μm
CO ₂ laser	stimulated emission lines	9-11 μm